

# Structure from motion for omnidirectional multi-camera system and its applications



Vision and Media Computing Lab.  
Graduate School of Information Science  
Nara Institute of Science and Technology (NAIST)

Tomokazu Sato

# Overview of this talk

- SFM and PnP for multi-camera system
  - SFM (Structure from motion)
  - PnP (Perspective n point) problem
- GPS integration to SFM
- Applications of omnidirectional SFM

## Applications of omnidirectional video using 3-D structure

(1) Omni-directional tele-  
presence system **without**  
**invisible area**



(2) **Novel-view synthesis** from  
omni-directional video using a  
deformable 3-D mesh model



(3) Feature landmark based  
marker-less **augmented reality**

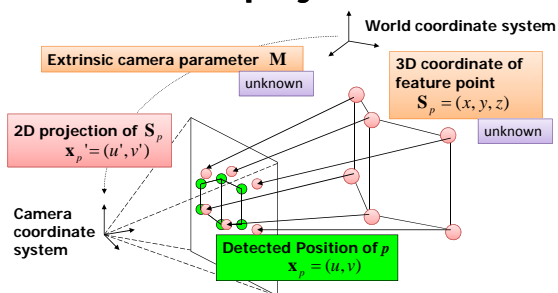


## Visual-SLAM (online SFM) and its application for video mosaic



\* T. Sato, A. Iketani, S. Ikeda, M. Kanbara, N. Nakajima, and N. Yokoya: 'Video mosaicing for curved documents by structure from motion', ACM SIGGRAPH2006, Sketches, Aug. 2006.

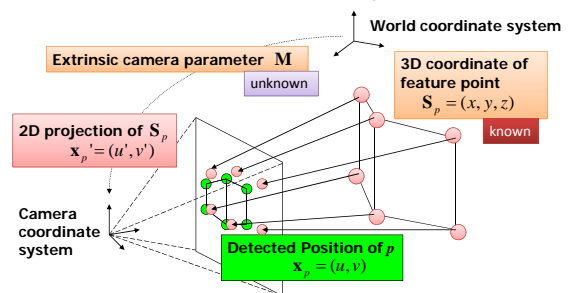
## SFM and Reprojection error



$$\text{Sum of re-projection errors: } E = \sum_p |x_p' - x_p|^2 \rightarrow \min$$

**Multiple images** are necessary to solve this problem.

## PnP problem and Reprojection error



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**Single images** is sufficient to solve this problem.

### Extrinsic camera parameter estimation (PnP and SfM)

- **PnP problem (Perspective n Point problem)**  
is for pairs of known 3-D positions and their 2-D observations.
  - Algebraic solution with minimum features (P3P, P4P, etc)
  - Linear solution for arbitrary number of features (PnP)
  - Non-linear minimization of reprojection errors  
(For final refinement, it needs good initial guess)
- **SfM (Structure from Motion)**  
is for unknown 3-D positions and their 2-D observations.
  - Factorization-based method (For video, batch processing)
  - Visual-SLAM (For video, real-time)
  - Ego-motion estimation (For sufficiently long baseline image pairs)
  - Non-linear minimization of reprojection errors  
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### Extrinsic camera parameter estimation (PnP and SfM)

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Solution for multi-camera system

Extension with GPS

### Basic strategy for visual-SLAM

Given 3-D positions of features (Reference points)

Camera positions and postures (Camera parameters)

```

    graph TD
      A[Feature tracking] --> B[Camera parameter estimation solving PnP]
      B --> C[3-D position update for image features]
      C --> D[Bundle adjustment]
      C -- Iterate for each frame --> B
  
```

### Linear solution for PnP problem in OMS (1/2)

Camera units of OMS

We minimize distances between projecting lines and 3-D position of features instead of reprojection errors.

### Linear solution for PnP problem in OMS (2/2)

$$A \mathbf{m} = \mathbf{s}$$

$$A = \begin{bmatrix} s1(k_1)S_1 & s2(k_1)S_1 & s3(k_1)S_1 \\ s1(k_2)S_2 & s2(k_2)S_2 & s3(k_2)S_2 \\ s5(k_1)S_1 & s6(k_1)S_1 & s7(k_1)S_1 \\ s5(k_2)S_2 & s6(k_2)S_2 & s7(k_2)S_2 \end{bmatrix}$$

$$\mathbf{s} = \begin{bmatrix} -s4(k_1) \\ -s4(k_2) \\ -s8(k_1) \\ -s8(k_2) \end{bmatrix}$$

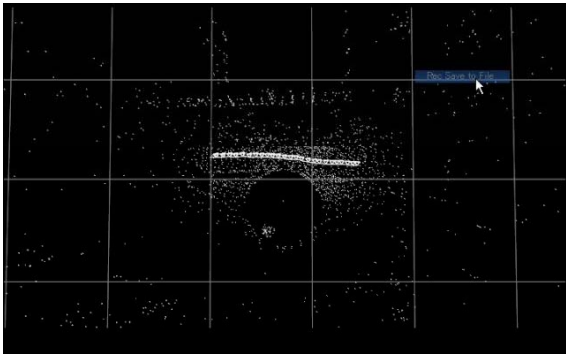
$$\mathbf{m} = (A^T A)^{-1} A^T \mathbf{s}$$

They can be computed from observations

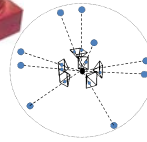
\* Tomokazu Sato, S. Ikeda, and N. Yokoya 'Extrinsic camera parameter recovery from multiple image sequences captured by an omni-directional multi-camera system', Proc. ECCV, May, 2004.

### Tracking of image features with reference points

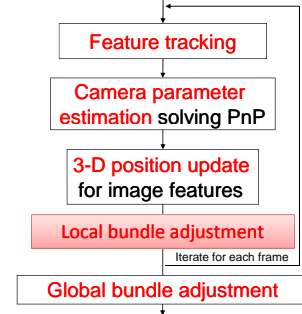
## Estimated camera path



## In case 3D reference points are unavailable



3D positions of features are initialized as they are on the sphere.

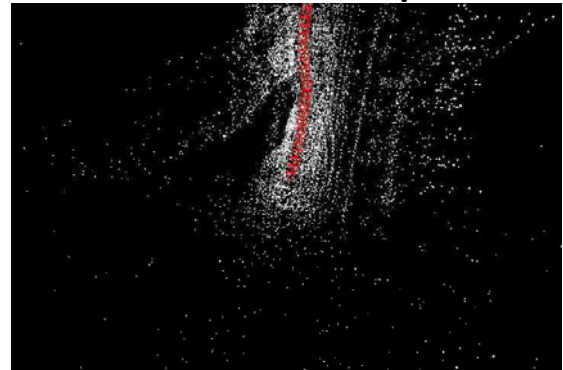


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## Tracking of image features without reference points



## Estimated camera path without 3D reference points



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## Extension of SFM

### Camera parameter estimation from video images and accuracy considered GPS

Hideyuki Kume,  
Tomokazu Sato, Naokazu Yokoya

\* 'Extrinsic camera parameter estimation using video images and GPS considering GPS positioning accuracy', *Proc. ICPR2010*, Aug. 2010 (accepted, to appear)

## Extension of objective function

Penalty term for GPS positioning is added to objective function.

$$E = \sum_{i \in F} \Phi_i + \omega \sum_{i \in F_g} \Psi_i$$

$\omega$ : weight

$F$ : Group of input frames

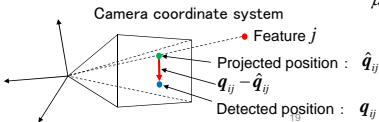
$F_g$ : Group of frames in which GPS data is acquired

$P_j$ : Group of feature points tracked in the  $i$ -th frame  
 $\mu_j$ : Confidence of feature  $j$

Reprojection error

$$\Phi_i = \frac{1}{|P_i|} \sum_{j \in P_i} \mu_j (q_{ij} - \hat{q}_{ij})^2$$

Penalty term for GPS positioning



## How should we design the penalty term for GPS data?

Positions are measured in fixed position using RTK-GPS (TOPCON GR-3) for 5 hours

Red axis: East, Green axis: South, Blue axis: Vertical up



Acquired positions in RTK-fix mode Length of axis: 1 [m]  
 Acquired positions in RTK-float mode Length of axis: 10 [m]

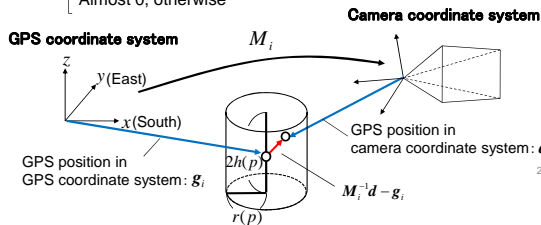
Assumption of normal distribution for GPS error in not effective for random walking errors for short time video streams.

## Penalty term for GPS positioning

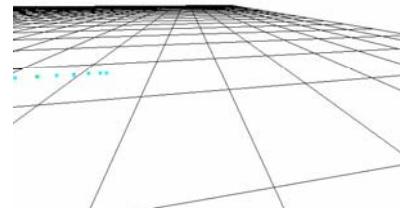
$$\Psi_i = \left( \frac{1}{r(p)} \sqrt{x_i^2 + y_i^2} \right)^{2n} + \left( \frac{1}{h(p)} z_i \right)^{2n}, \quad \begin{pmatrix} x_i \\ y_i \\ z_i \\ 1 \end{pmatrix} = M_i^{-1} d - g_i$$

$n$ : Large given number  
 $p$ : Confidence of GPS

$\Psi_i = \begin{cases} \text{Large number, if GPS is outside the cylinder} \\ \text{Almost 0, otherwise} \end{cases}$

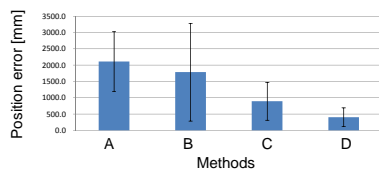
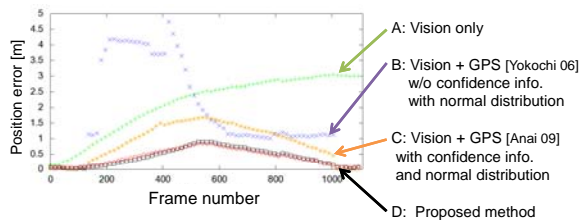


## Estimated camera paths



■ Proposed method  
 ■ Ground truth  
 ■ Compared method [Anai et al., 09]  
 ■ RTK-fix  
 ■ RTK-float  
 ■ Acquired GPS positions

## Quantitative evaluation



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### Application 1/3

## Omni-directional telepresence system without invisible area by image completion

**Koutaro Machikita, Norihiko Kawai, Tomokazu Sato, Naokazu Yokoya**

\*'Generation of an omnidirectional video without invisible areas using image inpainting', Proc. ACCV2009, Sep. 2009

### Invisible area in OMS



Omnidirectional telepresence system using video captured by OMS.

Complete video capturing for all the direction by OMS is essentially difficult.

Invisible area in the video decreases a reality



Image from Google's street view

Image completion technique that relying only for geometric info. often generates unnatural images.

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### Exemplar based image completion (image inpainting) methods

[Wexler et al., 2004]

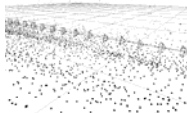


[Kawai et al., 2008]

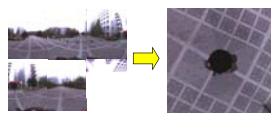


### Processes for image completion

1. Camera parameter estimation for omni-video



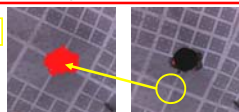
2. Estimation of ground surface and image projection to it



3. Determination of data region using geometric information



4. Image completion by using pattern similarity



Target

Reference frame

Target

Reference frame

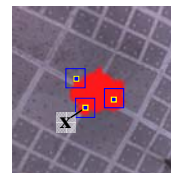
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### Image completion based on pattern similarity

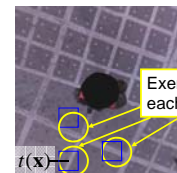
$$E = \sum_{\mathbf{x}_i \in \Omega} w_{\mathbf{x}_i} \left[ \sum_{\mathbf{p} \in W} \{I_f(\mathbf{x}_i + \mathbf{p}) - I_k(t(\mathbf{x}_i) + \mathbf{p})\}^2 \right]$$

$I(\mathbf{x})$  : Pixel value for  $\mathbf{X}$   
 $t(\mathbf{x})$  : Corresponded pixel position with  $\mathbf{X}$   
 $w_{\mathbf{x}}$  : Weight for  $\mathbf{X}$

Energy is defined as weighted sum of SSD.



Target frame  $f$



Reference frame  $k$

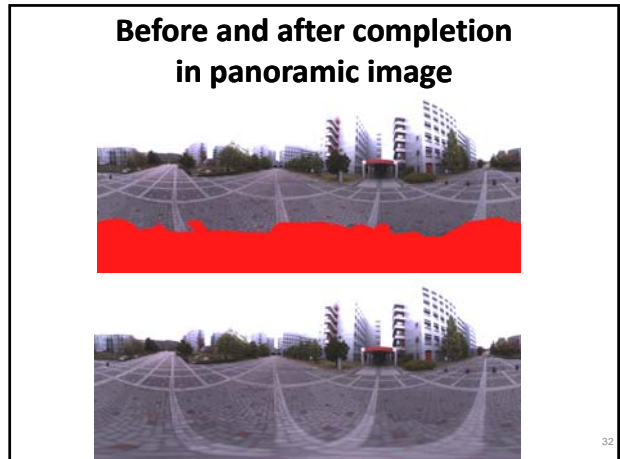
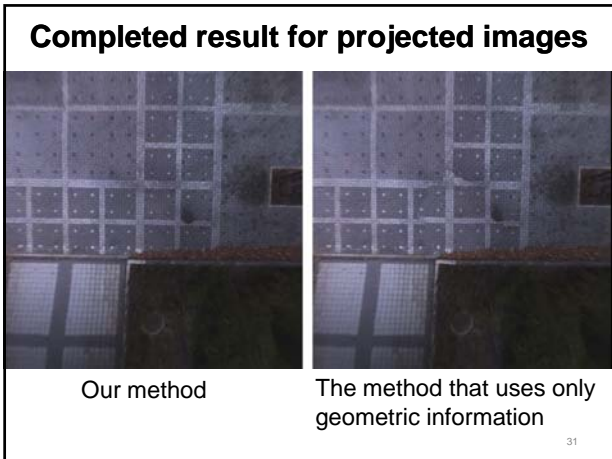
Exemplar for each pixel

Following two processes are repeated until energy convergence.

Searching for similar pattern



Update for pixel value

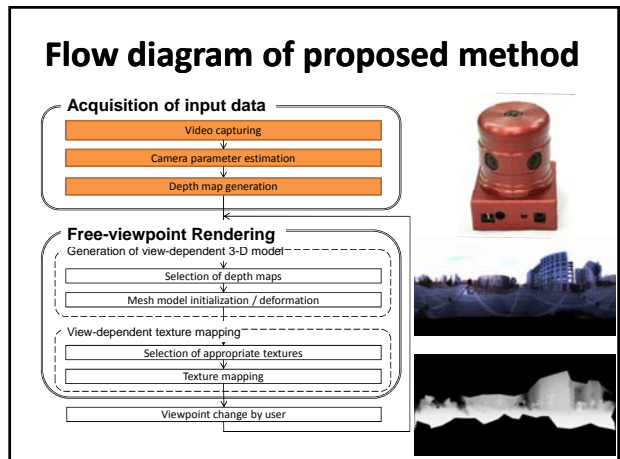
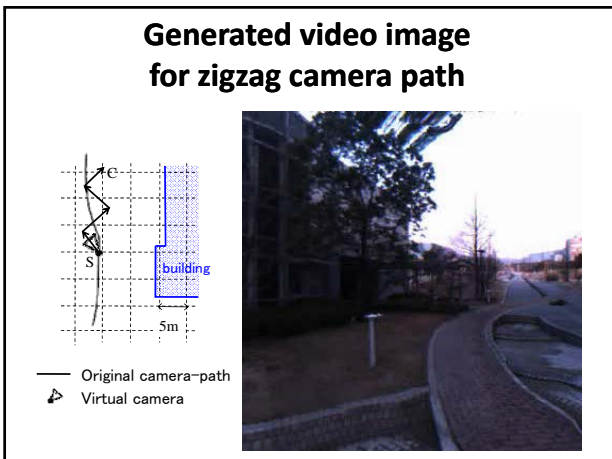


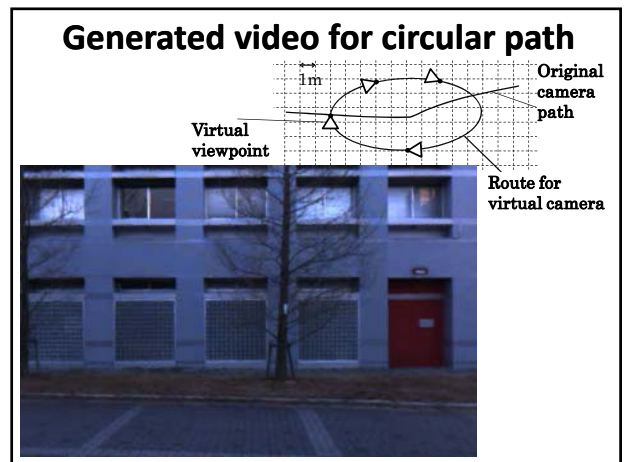
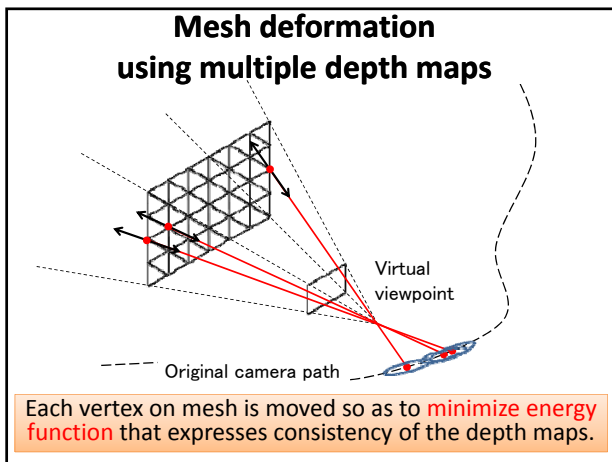
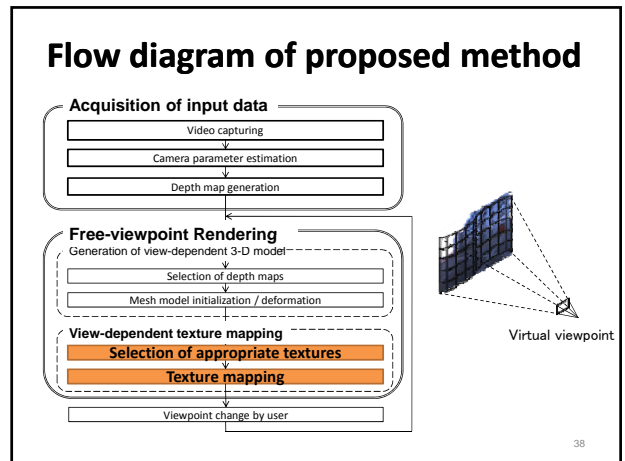
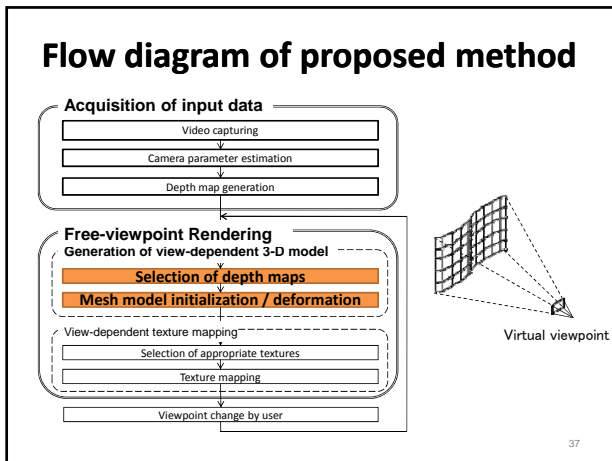
### Application 2/3

## Novel-view synthesis from omnidirectional video using a deformable 3-D mesh model

Hiroyuki Koshizawa, Takuya Ibuki, Tomokazu Sato, Naokazu Yokoya

\* 'Omnidirectional free-viewpoint rendering using a deformable 3-D mesh model', Int. J. of Virtual Reality, Vol. 9, No. 1, pp. 37-44, March 2010.





### Application 3/3

## Feature landmark based augmented reality

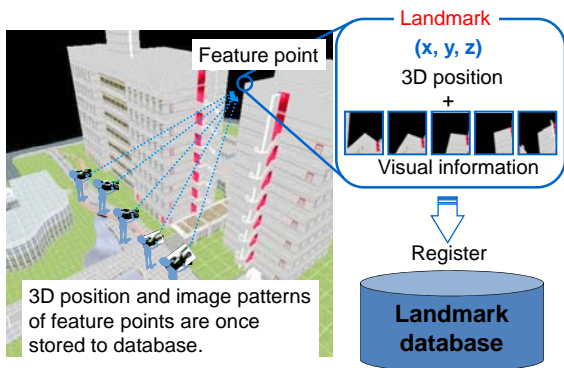
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**Takafumi Taketomi,**  
**Tomokazu Sato, Naokazu Yokoya**

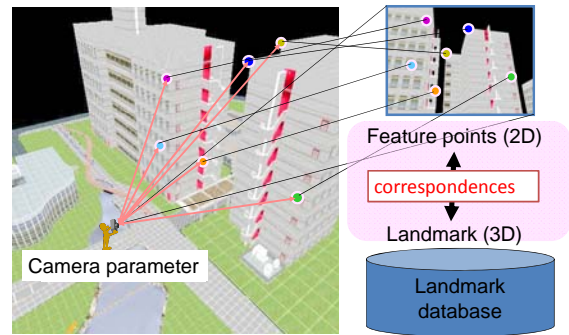
\* 'Real-time camera position and posture estimation using a feature landmark database with priorities', Proc. ICPR2008, Dec. 2008.



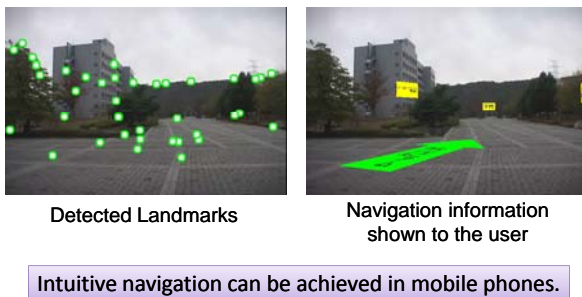
## Construction of landmark database



## Camera parameter estimation using landmark database



## Human navigation using Augmented Reality



## Application for car AR navigation



## Application for Pre-Visualization



## Summary

- Introduction of omnidirectional SFM
  - PnP Solution for OMS
  - Visual SLAM for OMS
- GPS integration to SFM
  - Cylinder whose size is changed depending on measurement confidence is used for penalty term.
- Applications of omnidirectional SFM
  - Video generation without invisible area
  - Novel view synthesis
  - Landmark based Augmented Reality

E-mail: tomoka-s@is.naist.jp

URL: <http://yokoya.naist.jp/~tomoka-s/index-e.html>